

# Reinforcement Learning

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## Exercise 4: Model-free Prediction

Nico Meyer

# Overview

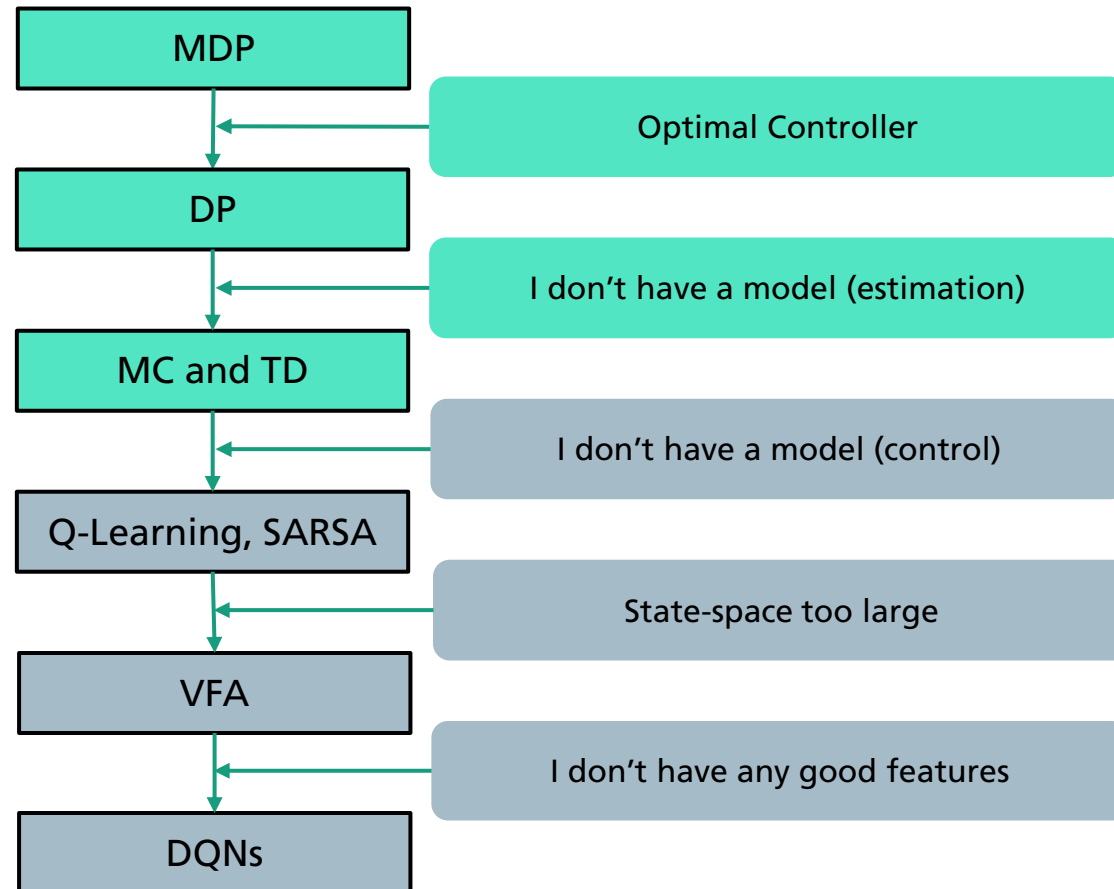
## Exercise Content

Week	Date	Topic	Material	Who?
0			<i>no exercises</i>	
1	23.04.	MDPs		Nico
2	30.04.	Dynamic Programming		Alex
3	07.05.	OpenAI Gym, PyTorch-Intro		Alex
4	14.05.	TD-Learning		Nico
5	22.05.	Practical Session (zoom@home)	<b>Attention: Lecture Slot!</b>	Nico + Alex
6	28.05.	TD-Control		Nico
7	04.06.	DQN		Nico
8	11.06.	VPG		Alex
9	18.06.	A2C		Nico
10	25.06.	Multi-armed Bandits		Alex
11	02.07.	RND/ICM		Alex
12	09.07.	MCTS		Alex
13	16.07.	BCQ		Nico



# Overview

## Overall Picture



# Recap


## Model-free Prediction



# Recap

## Monte Carlo and TD Methods

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- So far: We know our MDP model  $(\mathcal{S}, \mathcal{A}, \mathcal{P}, \mathcal{R}, \gamma)$ .
  - Planning by using dynamic programming
  - Solve a known MDP
- What if we don't know the model, i.e.,  $\mathcal{P}$  or  $\mathcal{R}$  or both?
- We distinguish between 2 problems for unknown MDPs:
  - **Model-free Prediction:** Evaluate the future, given the policy  $\pi$ .  
*(estimate the value function)* 
  - **Model-free Control:** Optimize the future by finding the best policy  $\pi$ .  
*(optimize the value function)*

# Recap

## Monte Carlo Policy Evaluation

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- MC Policy Evaluation
  - MC methods learn from episodes of experience under policy  $\pi$ :

$$s_t, a_t, r_t, s_{t+1}, \dots, s_{T-1}, a_{T-1}, r_{T-1}, s_T \sim \pi$$

- To evaluate a state  $s \in \mathcal{S}$  we keep track of the rewards received from that state onwards.
- **First-Visit** Monte-Carlo Policy Evaluation:
  - **First** time-step  $t$  that state  $s$  is visited in an episode
    - Increment counter  $N(s) \leftarrow N(s) + 1$ ,
    - Increment total return  $S(s) \leftarrow S(s) + G_t$ ,
    - Value is estimated by mean return:  $V(s) = S(s)/N(s)$
  - Our estimation  $V(s)$  will come close to  $V^\pi(s)$  as  $N(s) \rightarrow \infty$ .  
(considering the law of large numbers)

# Recap

## Temporal Difference Policy Evaluation

- Temporal-Difference Learning
  - Breaks up episodes and makes use of the intermediate returns
  - Learns from incomplete episodes (bootstrapping)
  - We update a guess towards a guess**

$$V^\pi(s) = \underbrace{r(s, \pi(s)) + \gamma \sum_{s' \in \mathcal{S}} \mathcal{P}(s'|s, \pi(s)) V^\pi(s')}_{\text{We don't know the transition model}}$$

We don't know the transition model

$$(s, a, r, s')$$

But we have real transitions available

$$V^\pi(s) = r + \gamma V^\pi(s')$$

Let's assume that the reality is the transition we observed

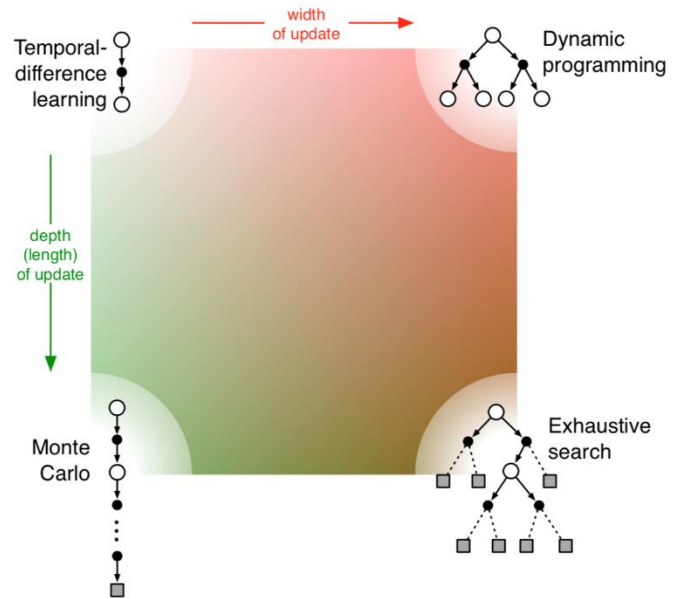
$$V(s) \leftarrow V(s) + \alpha(r + \gamma V(s') - V(s))$$

→ and update our old estimate “a bit” in this direction



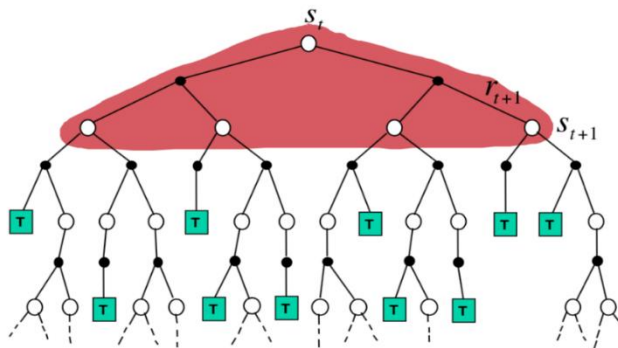
# Recap

## DP vs. MC vs. TD



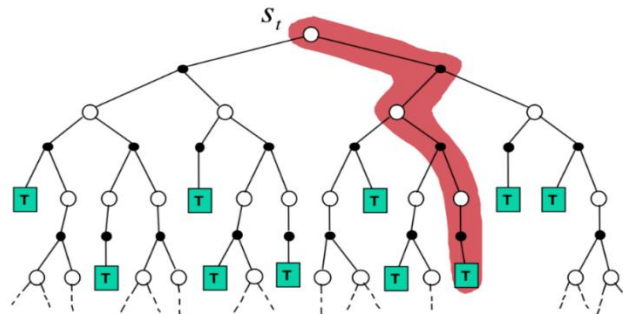
### DP Backup

$$V(S_t) \leftarrow \mathbb{E}_\pi [R_{t+1} + \gamma V(S_{t+1})]$$



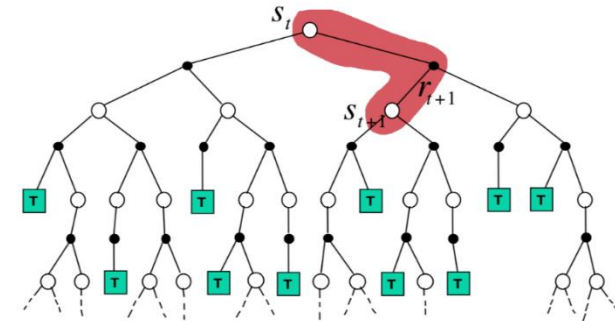
### MC Backup

$$V(S_t) \leftarrow V(S_t) + \alpha (G_t - V(S_t))$$



### TD Backup

$$V(S_t) \leftarrow V(S_t) + \alpha (R_{t+1} + \gamma V(S_{t+1}) - V(S_t))$$



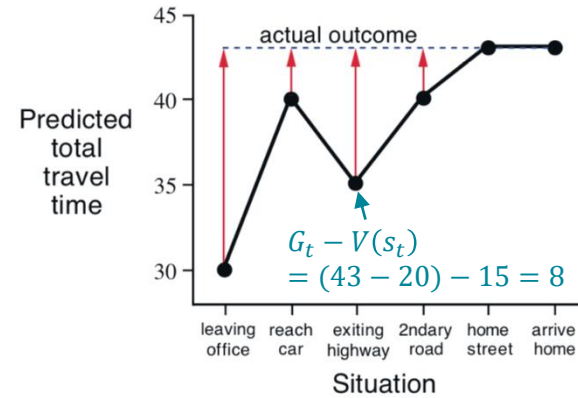
Sutton, R. S., & Barto, A. G. (2018). *Reinforcement learning: An introduction*. MIT press.



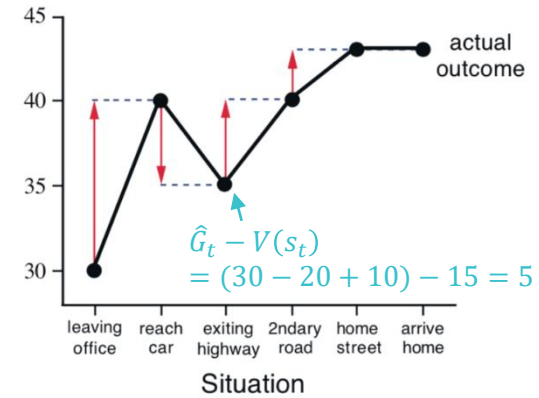
# Recap

## TD and MC Algorithms

MC ( $\alpha = 1$ )



TD ( $\alpha = 1$ )



Sutton, R. S., & Barto, A. G. (2018). Reinforcement learning: An introduction. MIT press.

### Tabular TD(0) for estimating $v_\pi$

Input: the policy  $\pi$  to be evaluated  
Algorithm parameter: step size  $\alpha \in (0, 1]$   
Initialize  $V(s)$ , for all  $s \in \mathcal{S}^+$ , arbitrarily except that  $V(\text{terminal}) = 0$

Loop for each episode:  
Initialize  $S$   
Loop for each step of episode:  
     $A \leftarrow$  action given by  $\pi$  for  $S$   
    Take action  $A$ , observe  $R, S'$   
     $V(S) \leftarrow V(S) + \alpha [R + \gamma V(S') - V(S)]$   
     $S \leftarrow S'$   
until  $S$  is terminal

### First-visit MC prediction, for estimating $V \approx v_\pi$

Input: a policy  $\pi$  to be evaluated  
Initialize:  
     $V(s) \in \mathbb{R}$ , arbitrarily, for all  $s \in \mathcal{S}$   
     $Returns(s) \leftarrow$  an empty list, for all  $s \in \mathcal{S}$

Loop forever (for each episode):  
    Generate an episode following  $\pi$ :  $S_0, A_0, R_1, S_1, A_1, R_2, \dots, S_{T-1}, A_{T-1}, R_T$   
     $G \leftarrow 0$   
    Loop for each step of episode,  $t = T-1, T-2, \dots, 0$ :  
         $G \leftarrow \gamma G + R_{t+1}$   
        Unless  $S_t$  appears in  $S_0, S_1, \dots, S_{t-1}$ :  
            Append  $G$  to  $Returns(S_t)$   
             $V(S_t) \leftarrow \text{average}(Returns(S_t))$

Sutton, R. S., & Barto, A. G. (2018). Reinforcement learning: An introduction. MIT press.

# Recap

## Advantages and Disadvantages of MC and TD

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- Which one should I use? Does it make any difference?
  - Bias/Variance Trade-Off
  - MC has high variance, but zero bias
    - good convergence (even with FA)
    - insensitive to initialization (no bootstrapping), simple to understand
    - only works for episodic problems (must wait until end of episode for update)
    - more efficient in non-Markov environments
  - TD has low variance, but some bias
    - TD(0) converges to  $\pi_v(s)$  (be careful with FA: bias is a risk)
    - sensitive to initialization (because of the bootstrapping)
    - update after each step
    - exploits Markov property and is more efficient in Markov environment
    - **usually more efficient in practice**

# Exercise Sheet 4

## Model-free Prediction



**Thank you for your attention!**